High-Energy Aqueous Magnesium Ion Batteries with Capacity-Compensation Evolved from Dynamic Copper Ion Redox

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The low specific capacity and low voltage plateau are significant challenges in the advancement of practical magnesium ion batteries (MIBs). Here, a superior aqueous electrolyte combining with a copper foam interlayer between anode and separator is proposed to address these drawbacks. Notably, with the dynamic redox of copper ions, the weakened solvation of Mg^{2+} cations in the electrolyte and the enhanced electronic conductivity of anode, which may offer effective capacity-compensation to the 3,4,9,10-perylenetetracarboxylic diimide (PTCDI)-Mg conversion reactions during the long-term cycles. As a result, the unique MIBs using expanded graphite cathode coupled with PTCDI anode demonstrate exceptional performance with an ultra-high capacity (205 mAh g⁻¹, 243 Wh kg⁻¹ at 5 A g⁻¹) as well as excellent cycling stability after 600 cycles and rate capability (138 mAh g⁻¹, 81 Wh kg⁻¹ at 10 A g⁻¹).

1. Introduction

Owing to the long cycle life, high cycling efficiency, and large energy density, lithium-ion batteries (LIBs) have triggered worldwide interest and been widely used for portable devices and electric vehicles during the past decades.^[1] Unfortunately, the prices of lithium salts have been increasing and recently exerted considerable pressure on the market^[2] and the limited crustal abundance of Li, Ni, and Co used for cathode materials cannot fulfill the boosting market needs.^[3] Besides, safety concerns regarding flammable electrolytes and thermal runaway have made them difficult to alleviate public concerns.^[4] Given

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these challenges, the development of lowcost and safe battery systems has become increasingly crucial and desirable.^[5] Recent years, multivalent ion (e.g., Mg^{2+,[6]} $Ca^{2+,[7]}$ and $Al^{3+[8]}$) batteries have been considered as promising alternatives to LIBs, because they have the potential to achieve higher theoretical energy densities than monovalent ion batteries. Among them, rechargeable magnesium batteries (RMBs) with Mg anode are particularly attractive due to the high volumetric energy density $(3833 \text{ mAh cm}^{-3})$, which is approximately twice that of lithium (2062 mAh cm⁻³).^[9] Additionally, Mg is one of the most abundant elements on earth (eighth in the earth's crust and third in seawater).

Although great effort has been devoted over the past decades, RMBs still suffer from two major challenges: i) the easy passivation of metal Mg anode, which makes it difficult to achieve a high Coulombic efficiency for magnesium electrolytes. While various types of specially designed Mg compatible electrolytes have been introduced to achieve reversible Mg plating-stripping,^[10] a steep cost, environmental harm, and low levels of anodic stability limit their broader application. Fortunately, this problem does not exist in magnesium ion batteries (MIBs) without magnesium metal; ii) the strong Coulombic interaction between the host materials and Mg²⁺ ions, which results in slow solid-state Mg²⁺ diffusions and large polarization effect, as well as low Mg²⁺ intercalation levels and rapid capacity decay.^[11] The slow Mg²⁺ diffusion can be alleviated by implementing partially crystalline/amorphous organic cathodes, where the conformational flexibility of polymeric chains can facilitate Mg²⁺ diffusion.^[12] On the other hand, the dual-ion batteries (DIBs) could be another effective approach to address this issue.

Unlike conventional batteries based on the shuttling back and forth of the same cations between the cathode and anode during charge–discharge cycles, DIBs allow both cations and anions to insert/de-insert into electrodes upon cycling.^[13] Specifically, the cations insert into the anode while the anions synchronously insert into the cathode during charging and vice versa. In DIBs, the ion diffusion kinetics could be improved due to the reduced diffusion distance. Besides, the working voltage can be increased (>4.5 V vs Li/Li⁺) and the cost can be decreased by using inexpensive graphite material of inserting anions as the cathode of DIBs. Particularly, Mg-ion-based DIBs

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(Mg-DIBs) that use a graphite cathode and an organic anode to accommodate ions could combine the benefits of MIBs and DIBs, and achieve high-rate capability and good stability. A Mg-DIB with 0.1 mol L⁻¹ magnesium trifluoromethanesulfonate (Mg(OTf)₂) in 1-butyl-3-methyl-imidazolium hexafluorophosphate (BMIMPF₆) ionic liquid obtained a capacity of 51 mAh g⁻¹ and 62% Coulombic efficiency after 60 cycles.^[14] The coupling of graphite cathode and TiNb₂O₅ anode with the electrolyte of magnesium bis(trifluoromethanesulfonyl)imide (Mg(TFSI)₂) in 1-butyl-1-methylpyrrolidinium bis(trifluoromethanesulfonyl) imide (Pyr14TFSI) can realize 60 mAh g⁻¹ at 3 C during 500 cycles.^[15] An organic Mg-DIB using polytriphenylamine (PTPAn) as the cathode, perylene diimide-ethylene diamine (PDI-EDA) as the anode and an anhydrous acetonitrile (AN) solution of magnesium perchlorate $(Mg(ClO_4)_2)$ as the electrolyte exhibits 73 mAh g⁻¹ capacity at a high current density of 1 A g^{-1.[16]} Recently, a Mg-DIB with a redox polymer (poly(vinyl carbazole), PVCz) cathode and an alloy-type (3Mg/Mg₂Sn) anode in Mg(TFSI)2/AN electrolyte was proposed, demonstrating 122 mAh g⁻¹ discharge capacity and the unprecedented high energy density (384 Wh kg⁻¹) and power density (6300 W kg^{-1}) at 1.5 A g⁻¹.^[12] Despite these great advancements, few of these strategies have brought about a near-practical improvement, especially because the obtained specific capacities are still much lower than practical standard, and the use of organic electrolytes could increase the battery cost and cause the safety problem.

Aqueous electrolytes have more advantages than organic electrolytes, such as higher safety, better environmental friendliness, lower cost, higher ionic conductivity, and faster ion diffusion kinetics.^[17] However, the relatively low charging cut-off voltage (<1.80 V) of aqueous electrolytes leads to low specific capacities. Aqueous/organic hybrid electrolytes inherit a fast dynamic and a wide voltage window from aqueous and organic electrolytes, respectively. The small amount of water introduced into the organic electrolytes could "shield" the charges of divalent Mg²⁺ ions and promote reversible Mg²⁺ insertion/deinsertion, consequently improving cycling stability and rate capability.^[18] It has been reported that Cu current collector or Cu interlayer was used to modify the electrochemical performance of Mg-S (Mg-Se) batteries.^[19] Formed sulfides (selenides) and the interaction between the Cu metal and magnesium polysulfides (polyselenides) play critical roles to the markedly improved reaction kinetics.^[19d,20] However, there were no relevant reports on the key role of Cu element in MIBs and Mg-DIBs.

In this study, we develop a Mg-DIB containing a expanded graphite (EG) cathode coupled with a 3,4,9,10-perylenetetracarboxylic diimide (PTCDI) anode and a novel hybrid aqueous/ organic electrolyte (1 mol L⁻¹ Mg(TFSI)₂ in deionized water and acetonitrile (AN)) with a Cu foam interlayer between anode and separator, as shown in Figure 1a. The unusual Mg-DIBs take the advantage of organic and aqueous solvent components such as a wide electrochemical window (Figure 1b) and fast ion diffusion kinetics, exhibiting high working voltage and rate capability, and a remarkable cycling stability. In addition, it was confirmed that Cu foam interlayer undergoes two consecutive redox steps: $Cu(0) \leftrightarrow Cu(I)$, $Cu(I) \leftrightarrow Cu(II)$, which offers effective capacity-compensation to the PTCDI-Mg conversion reactions. Moreover, the calculated results demonstrate that the existence of Cu²⁺ cations significantly reduces the interaction of Mg²⁺ cations with the solvent molecules and TFSI-, making Mg2+ cations to react with PTCDI more easily. Furthermore, in situ formation of metal Cu on the PTCDI anode improves the electronic conductivity of the organic anode, thus accelerating the promotion of the rate capability and long-term durability of the full cell. This innovative strategy opens a door for the practical application of rechargeable magnesium ion batteries with excellent electrochemical performance.

2. Results and Discussion

The hybrid electrolyte of 1 mol L⁻¹ Mg(TFSI)₂ in AN/H₂O at a 4.9:0.1 volume ratio displays a 4.47 V electrochemical window from -1.8 to 2.6 V versus Ag/AgCl (Figure 1b), which is wider than those with other AN/H2O ratios (such as 4.7:0.3, 4.5:0.5, and 4.0:1.0, Figure S1, Supporting Information). If not specially stated, the volume ratio of AN/H₂O in the hybrid electrolyte is 4.9:0.1 in this work. Such an electrochemical window is significantly wider than that of the aqueous electrolyte (2.05 V) and close to that of organic solution (5.23 V), as shown in Figure S2, Supporting Information. The electrochemical stabilization window of 4.47 V creates promising opportunities for improving the energy density of the full batteries. Compared with the organic and aqueous electrolytes (Figure S3, Sup1conductivity of 2.18 mS cm⁻¹, which is higher than the organic electrolyte (2.08 mS cm⁻¹) and close to the aqueous electrolyte (2.21 mS cm⁻¹), contributing the potential to obtain fast electrochemical kinetics.



Figure 1. a) Mg-DIB structure containing Cu foam interlayer; b) LSV curve showing the electrochemical window of the hybrid aqueous/organic electrolyte.

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The electrochemical performance of the Mg-DIBs full cell with EG cathode and PTCDI anode was further evaluated. When the potential exceeds 1.8 V (vs Ag/AgCl), the EG electrode would be oxidated to form CO₂.^[23] The cut-off voltage range of the full cell was set at 0.2-3.0 V considering the 2.8 V electrochemical window (marked in Figure 2a) between the EG cathode and the PTCDI anode. Because the mass loading of EG cathode is much larger than that of PTCDI anode (\approx 10:1), the electrochemical properties of the full cell mainly depend on that of PTCDI anode. Figure 2b shows the CV curves of the Mg-DIB full cell in the Mg(TFSI)₂ electrolyte with or without Cu foam interlayer at a scan rate of 5 mV s^{-1} in the voltage range of 0.2-3.0 V. Apparently, differing from that without Cu foam interlayer only having a couple of cathodic/anodic peak at $\approx 1.71/2.53$ V, the curve with Cu foam interlayer exhibits two sharpening peaks at ≈1.67/2.09 and 1.09/1.38 V during cycles,



Figure 2. a) CV curves for the 3rd cycle of PTCDI and EG electrodes at 5 mV s⁻¹ in a three-electrode system; b) typical CV curves of EG||PTCDI full cells with and without Cu foam interlayer at 5 mV s⁻¹; c) cycling performance of the full cells with and without Cu foam interlayer at a current density of 5 A g⁻¹; d) Coulombic efficiency of the full cells with and without Cu foam interlayer at 6 mV s⁻¹; c) cycles e) with Cu foam interlayer and f) without Cu foam interlayer at 5 A g⁻¹; g) rate capability of full cells with and without Cu foam interlayer from the current density of 5 to 10 A g⁻¹.

which could be assigned to the redox of Cu(0) \leftrightarrow Cu(I), and the reversible reaction of Mg²⁺ with PTCDI as well as the redox of Cu(I) \leftrightarrow Cu(II), respectively.

The cycling performance of Mg-DIB with or without Cu foam interlayer in the Mg(TFSI)₂ electrolyte is given in Figure 2c. When containing Cu foam interlayer, the cell is demonstrated to exhibit a reversible discharge capacity of around 205 mAh g⁻¹ (243 Wh kg⁻¹) at 5 A g⁻¹ in the voltage range of 0.2-3.0 V, much higher than that without Cu foam interlayer and conventional Mg-DIBs reported,^[12,14-16,24] and good cycling stability after 600 cycles. Due to the generation of Cu²⁺ cations from Cu interlayer in the first several cycles, the specific capacity of the cell gradually increases through a quick "activation" process, as shown in the highlighted area of Figure 2c. The halfbattery cycling performance with PTCDI electrode and copper foam interlayer was further evaluated via a three-electrode cell with Pt counter electrode and Ag/AgCl reference electrode in Figure S6, Supporting Information. The PTCDI electrode stabilized at around 210 mAh g⁻¹ specific capacity at 5 A g⁻¹, illustrating the contribution of copper ions to the capacity of the full cell. Compared to the increased capacity with high Coulombic efficiency at low current densities for the full cell without Cu interlayer, the capacity and Coulombic efficiency of the full cell with Cu interlayer decrease significantly at a lower current of 1 A g⁻¹ (Figure S7a, Supporting Information), which is probably related to some parasitic reactions caused by the continuous dissolution of Cu interlayer at low current densities. High-rate conditions to a certain extent lead to a suppression by shortening their retention time before the transformation into the final products (Figure S7b, Supporting Information). We also noticed that the Coulombic efficiency of Mg-DIB with Cu foam interlayer is much lower than that without Cu (Figure 2d). The functional mechanism of Cu foam interlayer in this Mg-DIB system will be discussed in detail below. Figure 2e,f shows the completely different charge-discharge curves at the 1st, 5th, 10th, 100th, and 150th cycles for the Mg-DIB with or without Cu foam interlayer, respectively. The voltage plateaus of chargedischarge curves exactly fulfill the peaks of CVs. Compared to that without Cu foam interlayer, the charge curves after the 10th cycle exhibit a short additional voltage profile from 1.3 to 1.6 V and a longer voltage profile from 2.0 to 2.5 V for the cell with Cu foam interlayer, corresponding to the reduction of Cu^{2+} to Cu^{+} and the mixed reaction (C=O groups in PTCDI to PTCDI-Mg as well as Cu(I) to Cu(0)) at anode side, respectively. Correspondingly, the discharge curves show a sloping voltage profile from 1.7 to 1.45 V and a short voltage profile from 1.0 to 0.93 V, related to the mixed oxidation reaction (PTCDI-Mg to C=O groups as well as Cu(0) \rightarrow Cu(I)) and Cu(I) \rightarrow Cu(II) at anode side, respectively. Meanwhile, EG cathode experiences a reversible insertion/deinsertion of TFSI⁻ during the charge/discharge process for the full cell with or without Cu foam interlayer. It also was notable that the "activation" process can be demonstrated in Figure 2e. Dynamic copper ion redox gradually emerges and exhibits a voltage plateau, which plays as capacity-compensation species and subsequently delivers good repeatability profiles after 100 cycles. Figure 2g exhibits admirable rate capability with a capacity of 40.9, 156.9, 163.4, 143.0, and 138.9 mAh g^{-1} at the varied current density of 5, 6, 7, 8, and 10 A g^{-1} with Cu foam interlayer. When the current

density returns to 5 A g⁻¹, the capacity achieves to 239.3 mAh g⁻¹, much greater than the initial capacity at the same current density, further confirming gradual activation process triggered by copper ion redox. The excellent recover capability indicates its superior rate performance of the EG||PTCDI full cell with Cu foam interlayer, while the cell without the interlayer exhibits much lower capacity, suggesting PTCDI anode could be not enough to react with Mg²⁺ ions and has poor electronic conductivity. Moreover, rate performance test after fully activation with Cu foam interlayer was conducted as exhibited in Figure S8, Supporting Information, the cell after fully activation with Cu foam interlayer still exhibits excellent rate performance.

To understand the two sharpening peaks related to the copper ions, we collect the CV results of full cell without Cu foam interlayer in Cu(TFSI)₂ electrolyte at a scan rate of 5 mV s⁻¹, as shown in Figure S9, Supporting Information. It is quite interesting that there is no difference between the curves with or without PTCDI anode, confirming that copper ions do not react with the PTCDI. Moreover, the CV curves exhibit two pairs of widen cathodic/anodic peaks at 1.58/2.68 and 0.93/1.62 V, which can be assigned with $Cu(0) \leftrightarrow Cu(I)$ and $Cu(I) \leftrightarrow Cu(II)$, respectively. It is notable that the area of the oxidation peak is much larger than that of the reduction peak, indicating that the charging capacity is much larger than the discharging capacity and thus a lower Coulombic efficiency is obtained. This could be attributed to the irreversibility of the redox process of copper ions. The cycling property of EG||PTCDI cells with Cu(TFSI)2 electrolyte is given in Figure S10, Supporting Information. The charging capacity of the first cycle is much larger than the discharging capacity, which proves the irreversibility of the redox process of copper ions, and the subsequent cycles are all in similarity (Figure S10a, Supporting Information, inset). The Coulombic efficiency is only about 20% during these cycles (Figure S10b, Supporting Information). The low Coulombic efficiency is due to the partial dissolution of metallic copper, which aligns with the prior report.^[25] Possible solutions to enhance the Coulombic efficiency include altering the solvents, incorporating ionic liquids, or introducing additives in the electrolyte to adjust the deposition morphology of copper.

The detailed morphology and the element distribution of the PTCDI anode obtained after charging EG||PTCDI cell were examined by high-angle annular dark field scanning transmission electron microscopy (HAADF-STEM), as displayed in Figure 3a-c. The brighter parts in the anode (Figure 3a) are related to PTCDI material because of its higher conductivity in gold grid. The PTCDI anode after charging exhibits an irregular structure, in which C, O, N, and Mg elements distribute evenly in the electrode (Figure 3b). Remarkably, Mg element enriches at the positions where the O and N elements are concentrated, which is associated with the formation of PTCDI-Mg through the Mg–O bonds. In order to prove the absence of Cu in the anode of the charged full cell, Cu element was added in the EDX mapping. It should be noted that we used gold grid to eliminate the influence of the carrier on the accuracy of EDX. As shown in Figure 3c, Cu element does not appear synchronously with any element of PTCDI, confirming that Cu hardly reacts with PTCDI active material. In addition, we primarily employed the first principles calculation to prove copper ions cannot react with PTCDI. Figure 3d presents the optimized





Figure 3. a) HAADF-STEM image, EDX mappings of b) C, O, N, Mg, and c) Cu for the PTCDI electrode after fully charging the EG||PTCDI cell with Cu foam interlayer and Mg(TFSI)₂ electrolyte. d) Unit cells of different PTCDI-Cu intercalation structures, the color codes for the atoms are as follows: blue, Cu; brown, C; red, O; gray, N, and white, H; e) the corresponding calculated formation energy of different PTCDI-Cu intercalation structures.

four PTCDI-Cu structures in different cases, and the corresponding calculated formation energy values are depicted in Figure 3e, the detailed data for the optimization structures are summarized in Table S1, Supporting Information. The formation energy is calculated by Equation (1):

$$E_{\rm f} = E_{\rm PTCDI+nCu} - E_{\rm PTCDI} - n \times E_{\rm Cu} \tag{1}$$

where *n* is the number of Cu atoms combined with PTCDI crystal, $E_{\text{PTCDI}+n\text{Cu}}$, E_{PTCDI} , and E_{Cu} are the DFT energies of the PTCDI crystal with the insertion of *n* Cu atoms, PTCDI crystal, and bulk Cu atoms, respectively. The optimized structures 1–4 are attached in the Supporting Information (separate file). When Cu ions are inserted into PTCDI, the calculation shows very high formation energy (>0 eV), proving that the reaction is unlikely to occur. In the CV curves at various cycles of the

EG||PTCDI full cell with Cu foam interlayer and Mg(TFSI)₂ electrolyte (Figure S11, Supporting Information), the first cycle curve is a bit different from the others, which could be ascribed to the generation of PTCDI-Mg at the anode side in the first charging process; and the formation of PTCDI as well as Cu(0) \rightarrow Cu(I) at around 1.65 V, Cu(I) \rightarrow Cu(II) at around 1.10 V in the first discharging process. The intensity of all the redox peaks enhances with the increase of cycles, indicating that the material experiences an activation process stimulated by the generated copper ions upon cycling.

In order to verify the functional mechanism of Cu foam interlayer in this Mg-DIB system, the CV measurement of the Cu foam in the Mg(TFSI)₂ electrolyte was carried out at a scan rate of 5 mV s⁻¹ in the voltage range of -2.0 to 3.0 V, with Cu foam as the working electrode, platinum as the counter electrode,

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copper ions in the $Cu(TFSI)_2 + Mg(TFSI)_2$ electrolyte due to the irreversibility of Cu to Cu^{2+} . The introduction of copper foam interlayer can make the concentration of copper ions in the electrolyte stable and enhance the electronic conductivity of PTCDI electrode via the copper layer on the electrode surface, thus increases the specific capacity and keeps the cycling process stable.

Furthermore, to investigate the effect of copper ions to magnesium ions in electrolyte, molecular dynamics (MD) simulations (Figure 4) were carried out to understand the interaction between cations/anions and solvent molecules. The radial distribution function (RDF) $g_{AB}(r)$, referring to the probability of finding another atom at a certain distance, can be used to represent the interaction between two components and evaluate the structures of the pure liquids and their mixtures.^[26] According to the RDFs, the Mg-N peak for Mg²⁺ with AN, Mg-N peak for Mg²⁺ with TFSI⁻, and Mg-H peak for Mg²⁺ with water in the electrolyte without Cu²⁺ cations correspond to the distance of 1.92, 1.95, and 2.34 Å, respectively (Figure 4b). Interestingly, in the electrolyte containing Cu²⁺ cations, the distance of Mg-N peak for Mg²⁺ with TFSI⁻ shows obvious change away from the centroid Mg²⁺ after Cu incorporation, and a much lower peak intensity of Mg-H peak for Mg²⁺ with water is observed simultaneously (Figure 4e), indicating fewer TFSI- and H₂O into the Mg²⁺ solvation sheath. The coordination number of Mg²⁺ with AN, H₂O, and TFSI⁻ decreases from 11.12, 11.33, and 9.8 to 10.72, 8.3, and 7.57 after the addition of Cu foam interlayer in the full cell, respectively. Therefore, Mg²⁺ cations in the electrolyte without Cu²⁺ are more likely to coordinate with solvent and TFSI⁻ anions than that containing Cu²⁺, which is consistent with the reduced solvation of Mg²⁺ cations in the electrolyte with Cu interlayer. Moreover, the corresponding 3D schematic diagrams of these two kinds of solvation structures also confirm TFSI⁻ anions and H₂O move away from the Mg²⁺ cations (Figure 4a,d), which further confirms that the solvation of Mg²⁺ cations is weakened. Thus, the calculated results demonstrate that the existence of Cu²⁺ cations significantly reduces the interaction of Mg²⁺ cations with the solvent molecules and TFSI⁻, making Mg²⁺ cations to react with PTCDI more easily. The variation of Mg²⁺ solvation structure after the addition of Cu foam interlayer was further studied by NMR spectroscopy. A downfield trend of Mg²⁺ peak can be observed in the ²⁵Mg NMR (Figure 4g) from the electrolyte after the addition of Cu foam interlayer, indicating the reduced Mg²⁺-solvent affinity. Figure 4c,f schematically summarizes the solvation structures of Mg²⁺ cations in the electrolytes without and with Cu²⁺ cations, respectively. These findings suggest that more relatively bare Mg²⁺ ions are present in the electrolyte with Cu foam interlayer during the electrochemical process, which further provides extra capacity to the reaction of PTCDI with Mg²⁺ ions.

In situ Fourier transform infrared spectroscope (FTIR) spectra, ex-situ X-ray photoelectron spectroscopy (XPS) and soft X-ray absorption spectroscopy (sXAS) of the PTCDI anode after fully charged EG||PTCDI full cell were measured for further investigating the specific reaction mechanism of anode side in this Mg-DIB system with Cu foam interlayer. To confirm the break of C=O bonds to form metallic bond during the charge process of the full cell, the PTCDI anode from the fully charged full cell was measured by XPS and the results are illustrated

shown in Figure S12a, Supporting Information, the solution turns light blue after the CV measurement, revealing that the Cu foam has experienced an electrochemical oxidation reaction to form Cu²⁺, whose color is exactly the same as the color of the Cu(TFSI)₂ (Figure S12b, Supporting Information). Thus, it can be concluded that Cu2+ ions are present in the form of Cu(TFSI)₂ after Cu foam is oxidized in the Mg(TFSI)₂ electrolyte. To eliminate the possibility that carbon paper current collector participates in the electrochemical reaction, carbon paper is alone used as the anode without PTCDI active material. The open circuit voltage of the full cell with EG cathode is around 0 V and remains little change after 2.5 h charging (Figure S13, Supporting Information), demonstrating that the carbon paper hardly delivers any capacity. When Cu foil is directly used as the anode current collector without Cu foam interlayer, the EG||PTCDI full cell effectively works less than 30 cycles along with similar specific capacities but lower Coulombic efficiencies than that using Cu foam interlayer and carbon paper anode current collector (Figure S14a, Supporting Information). We noticed that some floccule falls off from the PTCDI anode with the Cu foil current collector after the cycles. These floccule may be Cu(TFSI)₂ formed by the reaction of Cu current collector and the electrolyte via an electrochemical oxidation (Figure S14b, Supporting Information), making PTCDI material exfoliates from the Cu current collector, thus it is impossible to achieve long cycles. Therefore, carbon paper anode current collector and Cu foam interlayer are more suitable than Cu foil current collector in the Mg-DIB. This phenomenon has already demonstrated the key role of carbon paper anode current collector and Cu foam interlayer for the increased specific capacity and stable long-term cycles. Then, to reveal the existence of copper ions in the electrolyte during the electrochemical reaction process, the linear sweep voltammetry (LSV) measurement on the carbon paper electrode was carried out using platinum as the counter electrode, and standard Ag/AgCl electrode as the reference electrode at 5 mV s⁻¹ in the electrolyte obtained after CV cycles of the three-electrode cell (working electrode: Cu foam) in Mg(TFSI)₂ electrolyte (Figure S12a, Supporting Information). After continuous negative scans, red deposits can be clearly seen on the surface of the carbon paper, as shown in Figure S15a, Supporting Information. The morphology and component of the carbon paper after the negative scan process were investigated by Scanning electron microscopy (SEM) and X-ray diffraction (XRD) (Figure S15b, Supporting Information). Metal Cu is covered on the surface of the carbon paper to form a copper film, demonstrating the existence of copper ions and the electrochemical reduction of copper ion to metal Cu during the charge process of the full cell. In situ formation of metal Cu on the PTCDI electrode improves the electronic conductivity of the organic anode (from 131.03 to 643.97 S mm⁻¹), thus accelerating the promotion of the rate capability and long-term durability of the full cell. In addition, we evaluate the electrochemical performance of the Mg-DIBs full cell using the electrolyte containing both Cu(TFSI)₂ and Mg(TFSI)₂ without Cu foam interlayer, as shown in Figure S16, Supporting Information. The capacity reaches about 142 mAh g⁻¹ and remains stable during 100 cycles. However, the capacity decays rapidly after continuing the cycle, which can be ascribed to the limited

and standard Ag/AgCl electrode as the reference electrode. As

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Figure 4. Snapshots of the MD simulation boxes of the Mg(TFSI)₂ electrolytes a) without Cu^{2+} cations and d) with Cu^{2+} cations, insets are the representative solvation structures, colors for different elements: Cu, pink; Mg, light green; S, yellow; F, cyan; N, blue; O, red; H, white; and C, gray; RDFs g(r) (solid lines) and coordination number *N* (r) (dashed lines) of Mg–N and Mg–H pairs of the electrolytes b) without Cu^{2+} cations and e) with Cu^{2+} cations. Schematic diagrams of Mg²⁺ representative solvation structures for the electrolytes c) without Cu^{2+} cations and f) with Cu^{2+} cations. g) ²⁵Mg NMR of different electrolytes.

in Figure 5a,b. In C 1s spectra, there exist two peaks at 284.8 and 288.1 eV at the pristine state, corresponding to C=C and C=O bonds of PTCDI, respectively. At fully charged state, the characteristic peak of C=O bond weakens, meanwhile a new peak at 286.2 eV related to C-O bond emerges, suggesting the electrochemical reduction of carbonyl groups in PTCDI. In addition. O 1s characteristic peak of C=O bond at 531.3 eV for the pristine state vanishes, and a new peak at 532.7 eV corresponding to C-O bond appears (Figure 5b), which is in agreement with the aforementioned C 1s spectra results. The peak at 533.1 eV is attributed to oxygen of adsorbed H₂O in the outermost layer of the electrode.^[27] All peaks of C=O bonds in C 1s and O 1s spectra disappear completely, proving that carbonyl groups in PTCDI completely reacts with Mg²⁺. This is a key factor in increasing the specific capacity of the full cell. Moreover, we noticed that the intensity of N 1s characteristic peak at 400.0 eV corresponding to the N-H is gradually weakened after full charging (Figure S17, Supporting Information), which indicates the formation of hydrogen bond (N-H···O-C). Overall, these findings are in accordance with previously reported.^[28] Figure 5c,d shows the Cu-L, Mg-K sXAS spectra of the PTCDI anode from fully charged full cell. It is noted that the pristine PTCDI does not contain Cu and Mg element, while the Cu spectrum collected for the anode from the charged full cell shows six intense asymmetric peaks at 928.0, 932.5, 938.0, 942.0, 948.0, and 953.8 eV. The peaks at 932.5, 938.0, 942.0, and 953.8 eV are contributed to the so called L₃ and L₂ excitations of metallic Cu.^[29] Those at 928.0 and 948.0 eV correspond to the typical peaks of the Cu2+ L2.3-edge spectrum.[30] due to the partial retention of Cu^{2+} in the fully discharged anode. The Mg-K XAS shows an enhanced absorption intensity at 1310.0 eV,

which is related to the characteristic of bulk Mg–O.^[31] In the O-*K* sXAS of pristine PTCDI (Figure S18, Supporting Information), strong features around 532.0 and 535.0 eV arise from the carbonyl group. A probable contribution from CONH is expected in the energy range \approx 540 eV.^[32] After fully charging the cell, the characteristic peaks at 532.0 and \approx 540 eV weaken and the peak at 535.0 eV vanishes, demonstrating the reduction of the two C=O bonds.

Figure 5e shows the in situ FTIR spectra analysis of the PTCDI anode in the Mg-DIB at different charging/discharging states in the voltage range of 0.2–3.0 V. During charging process of the full cell, the peak at ~1681 cm⁻¹ primarily from the carbonyl groups (C=O) gradually weakens and a new peak at ~1608 cm⁻¹ originated from the C–O bond gradually strengthens, suggesting the conversion from carbonyl groups (C=O) to enolate groups (C–O). In addition, the reduction of the C=O bonds leads to a decreased π -conjugation in the PTCDI structure, as reflected by strengthened stretching vibrations of perylene ring and C=N from 1574 to 1500 cm⁻¹. Upon discharging process, all the above peaks recover to their original positions and intensities, revealing good reversibility of Mg insertion/extraction.

Based on these results, the Mg-ion storage mechanism of PTCDI in the Mg-DIB containing Cu foam interlayer is clear and largely dominated by gaining/losing electrons from the oxidation/reduction state of the organic conjugated moiety (C=O groups) and copper ion. The possible electrochemical evolution at PTCDI anode side during the charging/discharging of the full cell is as follows (Figure 5f): Charge: Stage I, the reduction of Cu(II) \rightarrow Cu(I); Stage II, the reduction of the carbonyl groups with Mg²⁺ in PTCDI and Cu(I) \rightarrow Cu(0); Discharge: Stage III, the oxidation of PTCDI-Mg to form the carbonyl

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Figure 5. a,b) C 1s, O 1s XPS analysis of pristine PTCDI and PTCDI anode from fully charged full cell; c) Cu L-edge and d) Mg K-edge sXAS spectra of PTCDI anode from fully charged full cell; e) in situ FTIR spectra of the PTCDI anode in the Mg-DIB under different charging/discharging states; f) the possible electrochemical evolution on anode side and the variation of PTCDI during the charge/discharge processes of EG||PTCDI full cell; g) performance comparison between this work and other previously reported Mg-DIBs and MIBs.

groups and Cu(0) \rightarrow Cu(I); Stage IV, the oxidation of Cu(I) \rightarrow Cu(II). A comparison with the electrochemical performance of Mg-DIBs^[12,15–16,24,28] and MIBs^[33] summarized in Figure 5g highlights the excellence of Mg-DIBs with Cu foam interlayer in this work. Our work introduces the copper ions into MIBs for the first time, enhances the deep understanding of copper ion in MIBs, and provides guidance for the development of dynamic ion redox toward high energy density of MIBs.

3. Conclusions

In this work, with a novel aqueous/organic hybrid electrolyte and a Cu foam interlayer between the anode and the separator, the MIB containing a PTCDI anode and a EG cathode realizes an ultra-high capacity (205 mAh g⁻¹, 243 Wh kg⁻¹ at a current density of 5 A g⁻¹), fourfold higher than those in conventional organic or aqueous electrolytes, as well as excellent cycling stability after 600 cycles and rate capability (138 mAh g⁻¹, 81 Wh kg⁻¹ at 10 A g⁻¹). Through first-principles calculations and in situ/ex situ characterizations, we found that the Mg-ion storage in PTCDI anode is dominated by gaining/ losing electrons from the oxidation/reduction state of the organic conjugated moiety. The dynamic redox of copper ions, the weakened solvation of Mg²⁺ cations in the electrolyte, and the enhanced electronic conductivity of anode offer effective capacity-compensation to the PTCDI-Mg conversion reactions during long-term cycles. These meaningful findings will

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provide a new avenue for the rational design of MIBs with a high energy density and a low cost.

4. Experimental Section

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Preparation of Electrodes: PTCDI anode was fabricated through grinding PTCDI powder (Meryer Chemical Technology Co., Ltd, >95.0%), carbon black (Super P) and polyvinylidene fluoride (PVDF) with a weight ratio of 7:2:1 in *N*-methyl-2-pyrrolidone (NMP) solvent to form a uniform slurry, and coating uniformly onto carbon paper (Toray) and drying at 80 °C under vacuum for 12 h. The expand graphite (EG) cathode was prepared by grinding EG powder (3Achem, particle size of 50 µm), Super P, and PVDF with a ratio of 8:1:1 in the NMP solvent to form a homogeneous slurry. The slurry was coated onto carbon paper and dried at 80 °C in vacuum for 12 h. Each cathode electrode contained active material with a mass loading of ≈2.0 mg cm⁻². The mass loading ratio of cathode to anode was ≈10:1.

Preparation of the Electrolytes: 1 mol L⁻¹ Mg(TFSI)₂ electrolytes in the organic, aqueous, or hybrid solvents of acetonitrile (AN)/H₂O were achieved through adding the predetermined amount Mg(TFSI)₂ (Huizhou Dado New Material Technology Co., Ltd, 99.5%) in AN (Aladdin), deionized water or AN/deionized water at the fixed volume ratios (4.9:0.1, 4.7:0.3, 4.5:0.5, and 4.0:1.0) under stirring for full dissolution in air, respectively. The Cu(TFSI)₂ electrolyte was prepared by adding 49.9 mg Cu(TFSI)₂ (Aladdin) into 2 mL AN/deionized water (4.9:0.1 volume ratio). The Cu(TFSI)₂ + Mg(TFSI)₂ electrolyte was prepared by adding 49.9 mg Cu(TFSI)₂ and 1.1692 g Mg(TFSI)₂ into 2 mL AN/deionized water (4.9:0.1 volume ratio).

Characterization: XRD measurements with Cu K α radiation were performed on a D/MAX-2200/PC Rigaku diffractometer. SEM used a JSM-7401F field-emission microscope, and HAADF-STEM with energy-dispersive x-ray spectroscopy was taken on a TALOS F200X microscope. Information on the functional groups of imidazole PTCDI was obtained by a FTIR (NICOLE6700). XPS analysis was conducted on an AXIS Ultra DLD with 284.8 eV C 1s line and monochromatic Al K α radiation. The sXAS measurements were carried out on the BL08U1A beamline at Shanghai Synchrotron Radiation Facility. The electronic conductivity measurement of the PTCDI electrodes with carbon paper was performed using a four-point probe tester (FT-371, Ningbo Rooko Instrument Co., Ltd.)

Electrochemical Measurements: CR2032 coin cells with a EG cathode, a glass fiber separator, a Cu foam interlayer, a PTCDI anode, and 1 mol L^{-1} Mg(TFSI)₂ in AN/H₂O electrolyte were assembled in air. Galvanostatic cycling and rate measurements were carried out with a 0.2–3.0 V cut-off voltage range on a Land battery test system. Cyclic voltammograms (CVs) were conducted on a CHI650C electrochemical workstation (CH Instruments Inc., Shanghai). The ionic conductivity of the electrolytes was measured by a conductivity instrument (DDS-307A).

Calculation Methods: In this work, DFT calculations of PTCDI-Cu were carried out by utilizing the projector augmented wave method^[34] implemented in the Vienna ab initio simulation package (VASP).^[35] The exchange-correlation function was described by the generalized gradient approximation^[36] with Perdew–Burke–Ernzerhof approach^[37] with an energy cut-off of 480 eV. The convergence criteria of energy was set to be 10⁻⁵ eV and a 6 × 2 × 3 Gamma centered k-mesh was adopted. During the process of geometric optimization for the PTCDI and PTCDI-Cu systems, cell parameters, cell shape, and atomic coordinates were free to change.

Molecular dynamics (MD) simulations were carried out by using the Forcite module with COMPASS force field for 1 mol L⁻¹ Mg(TFSI)₂ with solvent molecules (AN and H₂O), and the simulation box size was 40.6 × 40.6 × 40.6 Å. Cu²⁺ model contains 50 Mg²⁺, 50 Cu²⁺, 100 TFSI⁻, 938 AN, and 56 H₂O. Properties such as the RDF were obtained with the NVT ensemble at a volume determined by the NVE and NPH simulation. The temperature and the pressure were maintained at 298 K and 10⁻⁴ GPa, the time step and the total simulation time were 1 fs and 100 ps, and the number of steps was 5000 in NVT.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Data Availability Statement

The data that support the findings of this study are available in the supplementary material of this article.

Keywords

aqueous electrolytes, capacity-compensation, copper, high energy density, magnesium ion batteries

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- a) N. Nitta, F. Wu, J. T. Lee, G. Yushin, *Mater. Today* 2015, *18*, 252;
 b) J. M. Tarascon, M. Armand, *Nature* 2001, *414*, 359.
- [2] S. Yang, F. Zhang, H. Ding, P. He, H. Zhou, Joule 2018, 2, 1648.
- [3] C. Xu, Q. Dai, L. Gaines, M. Hu, A. Tukker, B. Steubing, Commun. Mater. 2020, 1, 99.
- [4] P. Sun, R. Bisschop, H. Niu, X. Huang, Fire Technol. 2020, 56, 1361.
- [5] a) A. Ponrouch, J. Bitenc, R. Dominko, N. Lindahl, P. Johansson, M. R. Palacin, *Energy Storage Mater.* **2019**, *20*, 253; b) P. Canepa, G. Sai Gautam, D. C. Hannah, R. Malik, M. Liu, K. G. Gallagher, K. A. Persson, G. Ceder, *Chem. Rev.* **2017**, *117*, 4287; c) Y. Liang, H. Dong, D. Aurbach, Y. Yao, *Nat. Energy* **2020**, *5*, 646.
- [6] a) L. Yin, B. J. Kwon, Y. Choi, C. J. Bartel, M. Yang, C. Liao, B. Key, G. Ceder, S. H. Lapidus, J. Am. Chem. Soc. 2021, 143, 10649;
 b) F. Xiong, Y. Jiang, L. Cheng, R. Yu, S. Tan, C. Tang, C. Zuo, Q. An, Y. Zhao, J.-J. Gaumet, L. Mai, Interdiscip. Mater. 2022, 1, 140.
- [7] J. Li, C. Han, X. Ou, Y. Tang, Angew. Chem., Int. Ed. 2022, 61, e202116668.
- [8] Y. Zhang, B. Zhang, J. Li, J. Liu, X. Huo, F. Kang, Chem. Eng. J. 2021, 403, 126377.
- [9] D. Wu, W. Ren, Y. NuLi, J. Yang, J. Wang, J. Mater. Sci. Technol. 2021, 91, 168.
- [10] a) Z. Zhao-Karger, R. Liu, W. Dai, Z. Li, T. Diemant, B. P. Vinayan, C. Bonatto Minella, X. Yu, A. Manthiram, R. J. Behm, M. Ruben, M. Fichtner, ACS Energy Lett. 2018, 3, 2005; b) J. Luo, S. He,



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T. L. Liu, ACS Energy Lett. 2017, 2, 1197; c) H. S. Kim, T. S. Arthur, G. D. Allred, J. Zajicek, J. G. Newman, A. E. Rodnyansky, A. G. Oliver, W. C. Boggess, J. Muldoon, Nat. Commun. 2011, 2, 427; d) O. Mizrahi, N. Amir, E. Pollak, O. Chusid, V. Marks, H. Gottlieb, L. Larush, E. Zinigrad, D. Aurbach, J. Electrochem. Soc. 2008, 155, A103; e) W. Ren, D. Wu, Y. N. NuLi, D. Zhang, Y. Yang, Y. Wang, J. Yang, J. L. Wang, ACS Energy Lett. 2021, 6, 3212; f) Y. Yang, Y. Qiu, Y. NuLi, W. Wang, J. Yang, J. Wang, J. Mater. Chem. A 2019, 7, 18295; g) W. Ren, D. Wu, Y. NuLi, X. Zhang, J. Yang, J. Wang, ACS Appl. Mater. Interfaces 2021, 13, 32957.

- [11] a) P. Saha, M. K. Datta, O. I. Velikokhatnyi, A. Manivannan, D. Alman, P. N. Kumta, *Prog. Mater. Sci.* **2014**, *66*, 1; b) E. Levi, Y. Gofer, D. Aurbach, *Chem. Mater.* **2010**, *22*, 860.
- [12] A. B. Ikhe, J. Y. Seo, W. B. Park, J.-W. Lee, K.-S. Sohn, M. Pyo, J. Power Sources 2021, 506, 230261.
- [13] M. Wang, Y. Tang, Adv. Energy Mater. 2018, 8, 1703320.
- [14] P. Seggem, S. N. Chavan, S. Biswas, V. R. Jetti, ACS Appl. Energy Mater. 2021, 4, 5165.
- [15] R. Yang, F. Zhang, X. Lei, Y. Zheng, G. Zhao, Y. Tang, C.-S. Lee, ACS Appl. Mater. Interfaces 2020, 12, 47539.
- [16] D. Lu, H. Liu, T. Huang, Z. Xu, L. Ma, P. Yang, P. Qiang, F. Zhang, D. Wu, J. Mater. Chem. A 2018, 6, 17297.
- [17] a) Y. Zhang, P. Nie, C. Xu, G. Xu, B. Ding, H. Dou, X. Zhang, *Electrochim. Acta* 2018, 268, 512; b) M. Pasta, C. D. Wessells, R. A. Huggins, Y. Cui, *Nat. Commun.* 2012, 3, 1149; c) Y. Xu, Z. C. Liu, X. H. Zheng, K. Li, M. M. Wang, W. Yu, H. L. Hu, W. Chen, *Adv. Energy Mater.* 2022, 12, 2103352.
- [18] a) J. Song, M. Noked, E. Gillette, J. Duay, G. Rubloff, S. B. Lee, *Phys. Chem. Chem. Phys.* **2015**, *17*, 5256; b) Y. Zhu, X. Guo, Y. Lei, W. Wang, A.-H. Emwas, Y. Yuan, Y. He, H. N. Alshareef, *Energy Environ. Sci.* **2022**, *15*, 1282; c) Y. Tang, X. Li, H. Lv, W. Wang, Q. Yang, C. Zhi, H. Li, *Angew. Chem., Int. Ed.* **2021**, *60*, 5443.
- [19] a) S. Zhang, Y. Huang, Y. NuLi, B. Wang, J. Yang, J. Wang, J. Phys. Chem. C 2020, 124, 20712; b) S. Zhang, W. Ren, Y. NuLi, B. Wang, J. Yang, J. Wang, Chem. Eng. J. 2022, 427, 130902; c) L. Zeng, N. Wang, J. Yang, J. Wang, Y. NuLi, J. Electrochem. Soc. 2017, 164, A2504; d) A. B. Du, Y. M. Zhao, Z. H. Zhang, S. M. Dong, Z. L. Cui, K. Tang, C. L. Lu, P. X. Han, X. H. Zhou, G. L. Cui, Energy Storage Mater. 2020, 26, 23.

- [20] a) P. He, H. O. Ford, L. C. Merrill, J. L. Schaefer, ACS Appl. Energy Mater. 2019, 2, 6800; b) A. Robba, M. Mežnar, A. Vizintin, J. Bitenc, J. Bobnar, I. Arčon, A. Randon-Vitanova, R. Dominko, J. Power Sources 2020, 450, 227672.
- [21] M. Shimizu, A. Nakahigashi, S. Arai, Phys. Chem. Chem. Phys. 2021, 23, 16981.
- [22] a) K. Beltrop, P. Meister, S. Klein, A. Heckmann, M. Grünebaum, H.-D. Wiemhöfer, M. Winter, T. Placke, *Electrochim. Acta* 2016, 209, 44; b) Z. Huang, Y. Hou, T. Wang, Y. Zhao, G. Liang, X. Li, Y. Guo, Q. Yang, Z. Chen, Q. Li, L. Ma, J. Fan, C. Zhi, *Nat. Commun.* 2021, 12, 3106.
- [23] H. Li, T. Kurihara, D. Yang, M. Watanabe, T. Ishihara, Energy Storage Mater. 2021, 38, 454.
- [24] Y. Zhu, J. Yin, A. H. Emwas, O. F. Mohammed, H. N. Alshareef, Adv. Funct. Mater. 2021, 31, 2107523.
- [25] C. Rousse, S. Beaufils, P. Fricoteaux, *Electrochim. Acta* 2013, 107, 624.
- [26] H. Takaba, W. Yamamoto, M. K. Alam, Bangladesh J. Phys. 2020, 27, 13.
- [27] B. Peng, T. Song, T. Wang, L. Chai, W. Yang, X. Li, C. Li, H. Wang, *Chem. Eng. J.* 2016, 299, 15.
- [28] X. Lei, Y. Zheng, F. Zhang, Y. Wang, Y. Tang, Energy Storage Mater. 2020, 30, 34.
- [29] F. Tavani, M. Fracchia, A. Tofoni, L. Braglia, A. Jouve, S. Morandi, M. Manzoli, P. Torelli, P. Ghigna, P. D'Angelo, *Phys. Chem. Chem. Phys.* **2021**, *23*, 26575.
- [30] R. Wang, X. Li, X. Han, J. Lin, Y. Wang, T. Qian, H. Ding, Y. Shi, X. Liu, Chin. Phys. B 2021, 30, 046102.
- [31] L. F. Wan, Y.-S. Liu, E. S. Cho, J. D. Forster, S. Jeong, H.-T. Wang, J. J. Urban, J. Guo, D. Prendergast, *Nano Lett.* **2017**, *17*, 5540.
- [32] F. Frati, M. O. J. Y. Hunault, F. M. F. de Groot, Chem. Rev. 2020, 120, 4056.
- [33] a) Z. Zhang, Y. Li, G. Zhao, L. Zhu, Y. Sun, F. Besenbacher, M. Yu, ACS Appl. Mater. Interfaces **2021**, 13, 40451; b) B. Wen, C. Yang, J. Wu, J. Liu, W. Wang, J. Yang, X. Chi, Y. Liu, Chem. Eng. J. **2022**, 435, 134997.
- [34] P. E. Blöchl, Phys. Rev. B 1994, 50, 17953.
- [35] J. Hafner, J. Comput. Chem. 2008, 29, 2044.
- [36] J. P. Perdew, W. Yue, Phys. Rev. B 1986, 33, 8800.
- [37] W. Kohn, L. J. Sham, Phys. Rev. 1965, 140, A1133.