

# Distributed Electric Vehicles Charging Management Considering Time Anxiety and Customer Behaviors

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**Abstract**—This paper proposes a charging management of electric vehicles (EVs) that considers time anxieties and different behaviors of EV customers. The time anxiety concept is newly presented to address some uncertain events that may happen meanwhile charging of EVs, affect their charging patterns, and prevent them from meeting their energy demands. The working principle of the concept relies on prioritizing the charging before the event occurrences, and thus changing the EV charging patterns. Based on this concept, four different EV customer behaviors are proposed and their influences are investigated. The EV charging problem is formulated as a generalized Nash equilibrium game, in which each EV minimizes its charging cost given its charging requirements and the charging facility constraints. The solution is developed on the basis of receding horizon optimization and reached iteratively in a distributed manner. Detailed simulation and comparison results are introduced to verify the effectiveness of the proposed charging management with the different time-anxiety-based EV customer behaviors.

**Index Terms**—Distributed charging management, electric vehicle (EV), time anxiety, customer behavior, game theory.

## NOMENCLATURE

$\mathcal{N}$	Number of EVs
$\mathcal{T}$	Time interval of EV charging
$T$	Number of time steps in EV charging interval
$t$	Specific time
$p_{g,t}$	Power of GS at time $t$
$p_{pv,t}$	Power of PVS at time $t$
$p_{b,t}$	Power of BESS at time $t$
$p_{l,t}$	Power of BLS at time $t$
$p_{n,t}$	Charging power of $EV_n$ at time $t$
$p_t^c$	Charging power capacity of EVCS at time $t$
$P_g^{max}$	Maximum power capacity of EVCS feeder
$\eta_t$	Overload safety factor at time $t$
$P_{n,t}^{min}$	Lower bound of $EV_n$ charging power at time $t$
$P_{n,t}^{max}$	Upper bound of $EV_n$ charging power at time $t$
$P_n^r$	Charger power rate of $EV_n$
$t_n^a$	Arrival time of $EV_n$ to EVCS

$t_n^d$	Departure time of $EV_n$ from EVCS
$\mathcal{T}_n^c$	Charging duration of $EV_n$
$E_n^a$	Energy of $EV_n$ when it arrives at EVCS
$E_n^d$	Energy of $EV_n$ when it departs from EVCS
$E_n^r$	Charging energy demand of $EV_n$
$SoC_{n,t}$	State of charge of $EV_n$ at time $t$
$SoC_n^a$	State of charge of $EV_n$ at the arrival time
$SoC_n^d$	State of charge of $EV_n$ at the departure time
$C_n$	Battery capacity of $EV_n$
$\eta_c$	Charging efficiency
$\Delta t$	Time step
$t_n^d'$	Starting time of $EV_n$ driver anxiety
$E_n^x$	Anxious energy of $EV_n$ driver
$\rho_n^s$	Electricity price sensitivity of $EV_n$ driver
$\rho_t$	Electricity price
$A'_{n,t}$	Influence of time anxiety of $EV_n$ driver
$A_{n,t}$	Normalized influence of $EV_n$ driver time anxiety
$B_{n,t}$	Basic influence of time anxiety of $EV_n$ driver
$A_n^{min}$	Lower bound of anxiety influence of $EV_n$ driver
$A_n^{max}$	Upper bound of anxiety influence of $EV_n$ driver
$\Delta A_{n,t}^i$	Impact difference resulted by the $i$ th behavior
$\lambda_{n,t}$	Lagrange multiplier of common constraint
$\mu_{n,t}^{min}$	Lagrange multiplier of $EV_n$ lower bound power
$\mu_{n,t}^{max}$	Lagrange multiplier of $EV_n$ upper bound power
$L_n$	Lagrangian function of $EV_n$ charging problem
$\bar{\lambda}_t$	Uniform Lagrange multiplier of common constraint
$\mathcal{P}[\cdot]$	Projection operator of an argument into a domain
$E_n^{x,th}$	Threshold of anxious energy of $EV_n$ driver

## I. INTRODUCTION

**D**UE to the energy demand growth and environmental concerns, renewable energy sources and electric vehicles (EVs) have received a prominent interest. This has increased the total charging load of EVs into the electric grid as EVs need to be charged frequently [1]. It is known that this total load should always respect the charging power capacity of the facility, e.g., charging station, to avoid creating overload cases that could affect its stability and efficiency [2]. Since the charging requirements of EVs are different due to the various demands of their customers, i.e., drivers, it is important to develop a charging management, i.e., control, that considers all the above issues properly in a dynamic charging environment.

The charging management of EVs was addressed in the literature for several aspects including the reduction of EV charging costs by controlling their charging schedules, i.e., power distribution, constrained to specific charging requirements. In this management, two control architectures can be

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mainly found, namely centralized and distributed approaches.

Ref. [3] centrally optimized the EV charging schedules with consideration of utility demand curtailment request. Ref. [4] presented a centralized scheme on the basis of learning particle swarm optimization for optimal EV charging schedules and economic benefits. Ref. [5] proposed a four-stage optimization control approach into EV charging station for operational cost reduction as well as supply and demanded power balance. On the other hand, the distributed control has also drawn a prominent concern because of its unique features. These features include communication burden reduction and customer privacy protection as it secures their private information. Ref. [6] implemented a game-theory-based approach for trade-off optimization between EV reserves provision and charging benefits. Ref. [7] proposed a fuzzy-logic-based approach for maintaining a power balance among the components of charging station. Ref. [8] applied a noncooperative game theory for EV charging cost minimization. The above existing control methods lacked detailed investigations on the power distribution among individual EVs, particularly under limited charging power capacity. Also, they did not represent the influences of uncertain events that may lead to rescheduling of charging power patterns. A further point is that the EV charging management should incorporate EV driver behaviors. These individual behaviors are usually very different, in terms of charging quantities and events. Modeling these behaviors in a systematic way is still ongoing research [9]–[15].

Ref. [11] investigated in the behavioral subscription of customers to a particular plan in the demand response management program. The development of the customer behavior was designed on the basis of logistic regression model and assumed attributes. Ref. [12] proposed a robust optimization method to address the customer behavior uncertainties in order to minimize comfort violation in household load scheduling. This method was simple in modelling and represented the behavior as additional constraints in the scheduling problem. Ref. [13] introduced a multi-objective optimization framework in EV charging stations that considered profitability improvement and customer satisfaction enhancement. The satisfaction of EV customers could be tuned by the shape parameters of the customer satisfaction model. Ref. [14] studied a competition-based method to determine the electricity price in electric vehicle charging stations. The EV customer behavior of selecting the charging station was formulated on the basis of electricity price, distance to charging station, and number of charging poles in charging station. Ref. [15] considered a customer behavior uncertainty in the household energy scheduling problem. The proposed model of customer satisfaction level was included as a set of constraints in this problem to reflect the comfort violation caused by customer behavior. In the aforementioned approaches, the customer behavior was modeled by a single mathematical formula, and then different customer behaviors could be represented by tuning parameters in this formula. In addition, some of these customer behavior models used their own proposed formulations but lacking theoretical justification. In order to provide more accurate descriptions, it is of interest to differentiate between customer behaviors by different unique mathematical formulas and include them into

the EV charging management problem.

Unlike the above literature, this paper introduces an EV charging management which addresses the aforementioned shortcomings. It formulates the EV charging problem on the basis of game theory with a charging cost minimization preference for each individual EV. It comprehensively studies the EV charging power distribution, i.e., EV charging patterns. Moreover, it proposes different EV customer behaviors and time anxiety concept that prioritizes the charging power of EVs before the occurrences of some uncertain events. Note that here EV customer, driver, and EV are all used as alternatives. The major work of this paper is summarized as follows:

- 1) A time anxiety concept of EV is newly proposed to mitigate the influence of uncertain events that may happen in the EV charging time durations and prevent EVs from meeting their energy demands.
- 2) Four different behaviors of EV customers are proposed and integrated into the EV charging management on the basis of the time anxiety concept and standard theoretical knowledge from social sciences and economics.
- 3) The dynamics of the time anxiety is systematically formulated and mapped to the proposed anxious energy, which is considered as the effect of the uncertain events on the EV customer charging requirements. Several case studies are presented to show the influences on the EV charging patterns including limited charging power capacity.

The rest of this paper is organized as follows. Section II models the system and the charging domain. Section III formulates the EV charging problem with the time anxiety and EV customer behaviors and develops the solution. Detailed simulation and comparison analyses are discussed in section IV. Finally, the conclusion is presented in section VI.

## II. SYSTEM MODEL AND CHARGING DOMAIN

As this paper focuses on charging EVs, the studied system is named as EV charging station (EVCS) which is considered as a distribution power network, part of the electric grid. This EVCS consists of several nodes (i.e., systems) which are connected together by power and communication lines as illustrated in Fig. 1. The first system is the grid system (GS) which represents the electric grid supply point. The other systems are a photovoltaic system (PVS), a battery energy storage system (BESS), and a base load system (BLS), in which each system could represent a group of systems of the same kind. The models of the PVS and the battery of BESS and EV are derived as in [16]–[18], and the BLS is considered as a building load demand, i.e., non-EV demand [19]. Moreover, there are a number of EVs ( $\mathcal{N} := \{1, 2, \dots, N\}$ ) which need to be charged and an EVCS operator whom addresses the following organizing missions:

- 1) Controls the power flow among GS, PVS, BESS, and BLS. Since the focus of this paper is on charging EVs, this power flow is controlled in a similar way of [5].
- 2) Broadcasts the charging power capacity, which indicates to the total available power for charging EVs, and checks its violation.

- 3) Helps in exchanging the public (i.e., shared) information between the aforementioned systems.

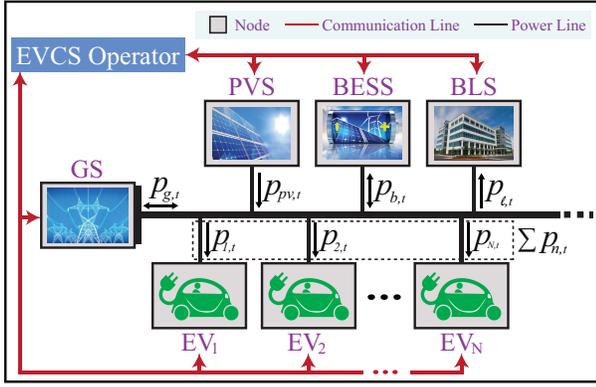


Fig. 1. Structure of the test system.

As shown in Fig. 1,  $p_{g,t}$ ,  $p_{pv,t}$ ,  $p_{b,t}$ , and  $p_{l,t}$  are the power flows of GS, PVS, BESS, and BLS, respectively at time  $t$ . Moreover,  $\sum_{n \in \mathcal{N}} p_{n,t}$  is the total charging power demand of EVs given that  $p_{n,t}$  is the charging power of  $EV_n$  at time  $t$ . After supporting the power demand of BLS, the total demand of EVs has to respect the charging power capacity of EVCS (i.e., charging domain)  $p_t^c$  as written in (1). This represents the common constraint that couples the charging schedules of EVs. If  $P_g^{max}$  is the maximum loading power capacity of EVCS feeder, which is related to the EVCS infrastructure, and  $\eta_t (\leq 1)$  is its overload safety factor [8], the charging power capacity of EVCS can be defined by (2). Thus, if (1) is violated, an overload case is occurred in the EVCS.

$$\sum_{n \in \mathcal{N}} p_{n,t} \leq p_t^c, \quad \forall t \in \mathcal{T}, \quad (1)$$

$$p_t^c = \eta_t (P_g^{max} + p_{pv,t} + p_{b,t} - p_{l,t}), \quad \forall t \in \mathcal{T}. \quad (2)$$

Moreover, if the lower and upper bounds of the  $EV_n$  charging power are  $P_{n,t}^{min}$  and  $P_{n,t}^{max}$ , respectively, then  $P_{n,t}^{min} \leq p_{n,t} \leq P_{n,t}^{max}$  has to be held, namely the instantaneous power constraint. As this paper addresses the charging problem of EVs,  $P_{n,t}^{min} = 0$  here. While, the upper bound equals the  $EV_n$  charger power rate  $P_n^r$  within the charging time duration and zero otherwise. This can be defined by (3) after considering  $t_n^a$  as the arrival time of  $EV_n$  to EVCS,  $t_n^d$  as its departure time from it, and  $\mathcal{T}_n^c$  as its charging duration, i.e.,  $t \in \mathcal{T} \cap [t_n^a, t_n^d]$ .

$$P_{n,t}^{max} = \begin{cases} P_n^r & t \in \mathcal{T}_n^c, \\ 0 & t \in \mathcal{T} \setminus \mathcal{T}_n^c. \end{cases} \quad (3)$$

If  $SoC_{n,t}$  is the state of charge (SoC) of  $EV_n$  at time  $t$ ,  $SoC_n^a$  is its SoC at the arrival time, and  $SoC_n^d$  is its SoC at the departure time, then (4) has to be held during charging. Given that  $C_n$  is the battery capacity ( $kWh$ ) of  $EV_n$ ,  $\eta_c \in (0, 1]$  is its charging efficiency, and  $\Delta t$  is the time step, the dynamic model of charging the EV on-board battery can be described by the linear model in (5).

$$SoC_n^a \leq SoC_{n,t} \leq SoC_n^d, \quad (4)$$

$$SoC_{n,t+1} = SoC_{n,t} + \frac{\eta_c p_{n,t} \Delta t}{C_n}. \quad (5)$$

It has to be noted that each  $EV_n$  has an energy request, i.e., demand,  $E_n^r$ . This energy can be written as in (6) given that  $E_n^a$  is  $EV_n$  energy when it arrives at EVCS and  $E_n^d$  is the energy that needs to be met before its departure time.

$$E_n^r = E_n^d - E_n^a = C_n (SoC_n^d - SoC_n^a) = T \sum_{t \in \mathcal{T}} p_{n,t}. \quad (6)$$

### III. EV CHARGING PROBLEM

The charging problem of each  $EV_n$  is defined to minimize its charging cost with consideration of the aforementioned charging domain. Since each  $EV_n$  has its own charging time duration, it has to be included in the charging problem. Moreover, in realistic scenarios, EV drivers may have different preferences (i.e., willing) to charge their EVs within these charging time durations. For example, some EV drivers are more anxious to charge their EVs at the early arrival periods to EVCS than others as they are afraid of meeting uncertain scenarios, i.e., events, that can happen in the later charging time periods. Such these events are the overload cases that constrain the EV charging power and the earlier departure times of EVs than scheduled from EVCS. These events may cause EVs to depart from EVCS without fulfilling their charging demands, and thus create worries (anxieties) to EV drivers meanwhile charging. Due to the human being nature, the degrees of these anxieties could be different among EV drivers, and thus their responses during charging will be different in order to relax their anxieties. Hence to make the charging problem more realistic, this anxiety and the resulted EV driver response (i.e., behavior) have to be included in the charging problem and to be addressed. This paper is dedicated to tackle this issue by proposing a time anxiety of EV driver that reflects the timely weighted concern to charge his/her EV within the charging duration  $\mathcal{T}_n^c$ . This anxiety leads the driver to secure more charging power in advance before possibly meeting the uncertain events. For clarity purposes, the influence of the proposed time anxiety is illustrated in Fig. 2. Here, Fig. 2(a) shows the original demanded charging power of  $EV_n$  in the charging duration without acknowledging the  $EV_n$  driver's anxiety; while Fig. 2(b) illustrates the modification in the demanded charging power when the  $EV_n$  driver responds to the anxiety. In the figure, it is assumed that the  $EV_n$  driver has anxiety about the occurrence of an event starting from  $t_n^{dt}$ , and  $[t_n^{dt}, t_n^d]$  is the anxious time interval. Thus, the charging energy during this interval is defined as an anxious energy  $E_n^x$ . Note that  $\Delta t$  is the time step, and  $t$  ranges here within the anxious time interval.

$$E_n^x = \Delta t \sum_{t \in [t_n^{dt}, t_n^d]} p_{n,t}. \quad (7)$$

This energy represents the charging amount that the EV driver is anxious to possibly miss due to the event occurrence. As a result,  $EV_n$  will try to shift part or all of the charging energy demand (i.e., shifted energy) from the anxious time interval to earlier time periods, as seen in Fig. 2(b). This will mitigate or cancel the anxiety of  $EV_n$  driver if the remaining anxious energy,  $E_n^x$ , is close to or lower than its threshold.

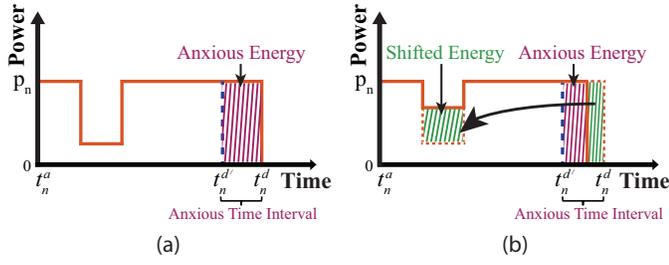


Fig. 2. Concept of the charging power of EVn. (a) Without time anxiety. (b) With time anxiety.

### A. Problem Formulation

As each  $EV_n$  seeks to reserve its own preference, i.e., minimizes its charging cost (\$), the charging problem is formulated as a noncooperative game-theoretic problem. Given that  $\rho_n^s$  is the electricity price sensitivity ( $\$/(\text{kWh})^2$ ) of  $EV_n$ ,  $\Delta t$  is the time step ( $h$ ),  $p_{n,t}$  is the charging power ( $\text{kW}$ ) of  $EV_n$ ,  $\rho_t$  is the electricity price ( $\$/\text{kWh}$ ), and  $A_{n,t}$  is the influence of the time anxiety (dimensionless as seen in (11)-(13)), the charging problem of each  $EV_n$  is defined as follows,

$$\min_{p_{n,t}} \sum_{t \in \mathcal{T}} A_{n,t} \left( \frac{1}{2} \rho_n^s \Delta t^2 p_{n,t}^2 + \rho_t \Delta t p_{n,t} \right), \quad (8)$$

$$\text{s.t.} \sum_{n \in \mathcal{N}} p_{n,t} \leq p_t^c, \quad \forall t \in \mathcal{T}, \quad (9)$$

$$P_{n,t}^{\min} \leq p_{n,t} \leq P_{n,t}^{\max}, \quad \forall t \in \mathcal{T}. \quad (10)$$

Since the EV charging problem is formulated on the basis of game theory and given that the constraint (9) couples all the charging power demands of EVs, this problem is actually a generalized Nash equilibrium (GNE) problem [20]. As designed by the cost function (8), a larger electricity price will lead to a lower charging power. Moreover, from a mathematical perspective if the driver has a big anxiety to charge his/her EV, i.e., needs to have a high charging power, then  $A_{n,t}$  has to be small. Given the discussion early this section, the anxiety at the early charging time duration is expected to be higher than at the late duration to prioritize the charging before the event occurrence. Then, the value of  $A_{n,t}$  increases gradually over the charging time duration as basically defined by (11) and shown in Fig. 3(a). As this paper investigates in the EV driver behavior, it further proposes four different behaviors on the basis of (11), namely non time anxious driver (NTAD), less time anxious driver (LTAD), mid time anxious driver (MTAD), and high time anxious driver (HTAD) as defined by (12) and illustrated in Fig. 3(b)-(c). The function formulation of each behavior type is selected on the basis of insights from social sciences and economics [21]. It has to be noted that NTAD represents the careless behavior of EV driver to the anxious energy, which is the common model in the EV charging problem literature.

$$B_{n,t} = \min \left( \frac{\max(t - t_n^a, 0)}{t_n^d - t_n^a}, 1 \right). \quad (11)$$

$$A'_{n,t} = \begin{cases} A_n^{\max} \times 1 & \text{for NTAD,} \\ A_n^{\max} \times \ln[B_{n,t}(e-1) + 1] & \text{for LTAD,} \\ A_n^{\max} \times B_{n,t} & \text{for MTAD,} \\ A_n^{\max} \times \frac{e^{B_{n,t}} - 1}{e-1} & \text{for HTAD.} \end{cases} \quad (12)$$

Note that  $A_n^{\max}$  is the upper bound of the anxiety influence which is assumed to be one for normalization purposes. In general cases, the lower bound  $A_n^{\min}$  may have any value in the range  $[0, A_n^{\max}]$ , thus a transformation is applied on (12) as defined by (13) and shown in Fig. 3(d).

$$A_{n,t} = \left( \frac{A_n^{\max} - A_n^{\min}}{A_n^{\max}} \right) \times A'_{n,t} + A_n^{\min}. \quad (13)$$

It is clear from Fig. 3 that the anxiety influence of LTAD (i.e.,  $A_{n,t}^{LTAD}$ ) is bigger than that of MTAD (i.e.,  $A_{n,t}^{MTAD}$ ) in which is bigger than that of HTAD (i.e.,  $A_{n,t}^{HTAD}$ ), and all are smaller than that of NTAD (i.e.,  $A_{n,t}^{NTAD}$ ). It is worthy to note that the value of  $(A_n^{\max} - A_n^{\min})$  is actually the EV driver time anxiety, i.e., time anxiety depth. This explains the relationship of the smaller (i.e., closer to zero) value of  $A_n^{\min}$  is, the bigger time anxiety of EV driver is. Also, a smaller  $A_n^{\min}$  leads obviously to a smaller  $A_{n,t}$ . Again, the bigger anxiety leads to larger willing of EV driver to fulfill his/her charging demand as early before approaching the departure time, and thus to lower the amount of the anxious energy.

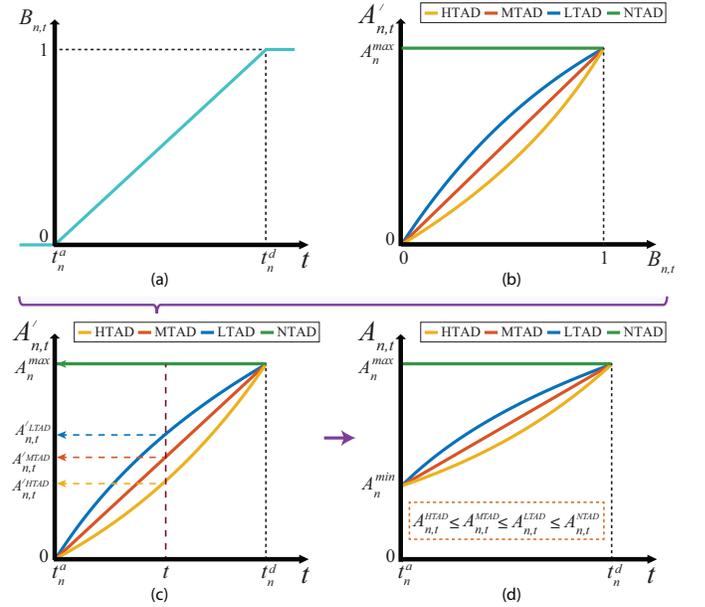


Fig. 3. (a) Dynamics of the basic anxiety influence over time. (b) Anxiety influence vs. its basic value under different behaviors of EV drivers. (c) Anxiety influence vs. time. (d) Modified scale of anxiety influence vs. time.

Based on the aforementioned discussions, the time-anxiety-based behavior of EV driver is determined by two factors. The first is the time anxiety depth and the second is the curve shape, i.e., behavior type. For clarity of the latter point along with the indicative meanings of the selected behavior names, their influences are illustrated in Fig. 4 given the same time anxiety depth. Here, the fixed anxiety influence of NTAD, i.e.,  $A_n^{\max}$ , is chosen as a reference value as shown in Fig. 4(a).

The difference between it and the anxiety influence which is resulted by the proposed behavior is considered as the impact difference. For example,  $\Delta A_{n,t}^{LTAD} = A_n^{max} - A_{n,t}^{LTAD}$  is the impact difference (i.e. modification) resulted by the LTAD behavior. As seen in Fig. 4(b), the LTAD behavior scales down the reference anxiety influence during the charging time duration by different weighted values that reflect the anxiety dynamics of EV driver within this duration. Meanwhile, and as indicated by the name, the MTAD behavior scales down more the reference anxiety influence as he/she has a bigger anxiety for charging as depicted in Fig. 4(c). Comparing with LTAD and MTAD and as seen in Fig. 4(d), HTAD has the largest impact in lowering the reference anxiety influence. Thus, this driver is most willing driver, i.e., competitor, among others to charge his/her EV during the charging duration to reduce the amount of his/her anxious energy, and accordingly (14) holds.

$$\Delta A_{n,t}^{NTAD} \leq \Delta A_{n,t}^{LTAD} \leq \Delta A_{n,t}^{MTAD} \leq \Delta A_{n,t}^{HTAD}. \quad (14)$$

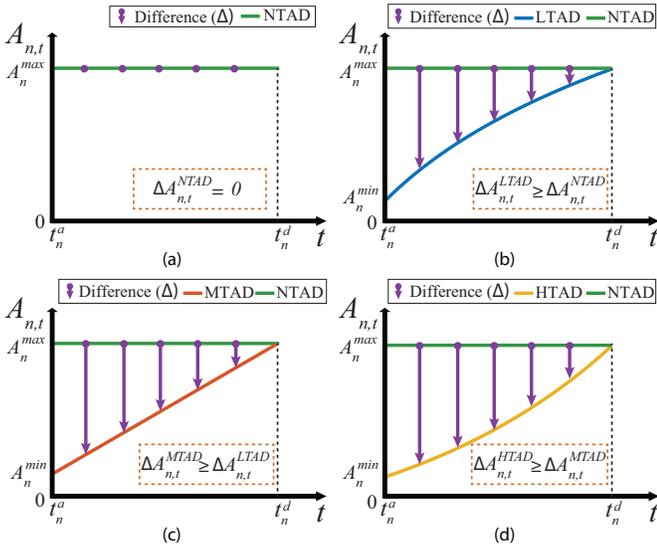


Fig. 4. (a) Reference anxiety influence of NTAD. (b) Modified anxiety influence of LTAD. (c) Modified anxiety influence of MTAD. (d) Modified anxiety influence of HTAD.

## B. Problem Solution

As known, the charging environment is dynamic in which some uncertain events could happen meanwhile charging. Thus, addressing the charging problem over  $T$  time steps rather than a single one is valuable to determine the amount of anxious energy and to take the actions of changing the EV charging patterns in advance. Hence the solution of the EV charging problem in this paper is formulated on the basis of receding horizon optimization [22]. In this framework, the optimization process is calculated over the  $T$  time steps, however, only the first optimal action is applied at the current time step. In the next time step the optimization process will be implemented again with one-time-step shifted horizon and with newly updated and available information. The optimization process is formulated on the basis of Karush–Kuhn–Tucker

(KKT) conditions of optimality. Thus, given that  $\lambda_{n,t}$ ,  $\mu_{n,t}^{min}$ , and  $\mu_{n,t}^{max}$  are the Lagrange multipliers, the Lagrangian function of the EV charging problem, i.e., (8), (9), and (10), for each  $EV_n$  can be introduced by (15). If a bold style of a symbol is introduced to refer to its values over  $T$  time steps, i.e.,  $T \times 1$  vector, the gradient condition of KKT necessary optimality conditions can be then given by (16).

$$\begin{aligned} L_n = & \sum_{t \in \mathcal{T}} A_{n,t} \left( \frac{1}{2} \rho_n^s \Delta t^2 p_{n,t}^2 + \rho_t \Delta t p_{n,t} \right) \\ & - \sum_{t \in \mathcal{T}} \lambda_{n,t} \left( \sum_{n \in \mathcal{N}} p_{n,t} - p_t^c \right) \\ & + \sum_{t \in \mathcal{T}} \mu_{n,t}^{min} (P_{n,t}^{min} - p_{n,t}) + \sum_{t \in \mathcal{T}} \mu_{n,t}^{max} (p_{n,t} - P_{n,t}^{max}), \end{aligned} \quad (15)$$

$$\begin{aligned} \frac{\partial L_n}{\partial p_n} = & \mathbf{A}_n (\rho_n^s \Delta t^2 p_n + \rho \Delta t) - \lambda_n + \mu_n^{min} + \mu_n^{max} \\ = & 0. \end{aligned} \quad (16)$$

It has to be noted that the KKT necessary conditions of this problem are sufficient as the problem is convex due to convexity of the cost function and the linear constraints. Thus, since the charging problem is GNE problem, the existence and uniqueness of its Nash equilibrium (NE) can be then proofed. As the most socially stable equilibrium is of interest here, the Lagrange multipliers of the common constraint (9) of all EVs have to share the same value, i.e.,  $\bar{\lambda}$  [23]. This NE can be expressed by (17) in which  $p_n$  is between  $P_n^{min}$  and  $P_n^{max}$ . Hence the  $\bar{\lambda}$ -based solution can be uniquely presented by (18) given that  $\mathcal{P}[\cdot]$  is a projection operator of the argument into the  $EV_n$  feasible charging domain, i.e., respecting its local constraint (10).

$$\mathbf{A}_n (\rho_n^s \Delta t^2 p_n + \rho \Delta t) \doteq \bar{\lambda}, \quad (17)$$

$$p_n = \mathcal{P} \left[ \frac{\bar{\lambda}}{\rho_n^s \Delta t^2} - \rho \Delta t \right]. \quad (18)$$

To reach this solution, all the information in (18) including  $\bar{\lambda}$  and  $\mathbf{A}_n$  have to be known. If a centralized control method is the case here, all these information have to be revealed to its global controller to allow it assigning the charging power of each EV. However, since securing the privacy is of concern here, this centralized method turns out to be invalid. This issue becomes more critical in practice after including the EV driver behavior which is a unique private information. As a result, a distributed charging management is proposed here in which the charging decisions of EVs are made by themselves through their local controllers. Each local controller needs to reach the solution of (18) on the basis of its local information, i.e.,  $\mathbf{A}_n$ ,  $\rho_n^s$ , and  $\lambda_n$ , as well as the global shared ones of  $\rho$  and other neighboring EVs'  $\lambda$ 's (i.e.,  $\mathcal{N}_n$ ). As mentioned early section II, each  $EV_n$  in the EVCS is considered as a node in which all the nodes including that of EVCS operator are connected by communication links and the resulting network can be illustrated in Fig. 5. The shared (i.e., public) information between the nodes are shown here and the organizing

missions of EVCS operator are the three ones discussed in section II. Moreover, each  $EV_n$  executes algorithm 1, which is the proposed distributed charging management with the time anxiety concept (DCMTA). For clarity in the description, this algorithm is divided into four tasks with meaningful names that indicate to their functions, namely initialization, optimization, modification, and communication tasks.

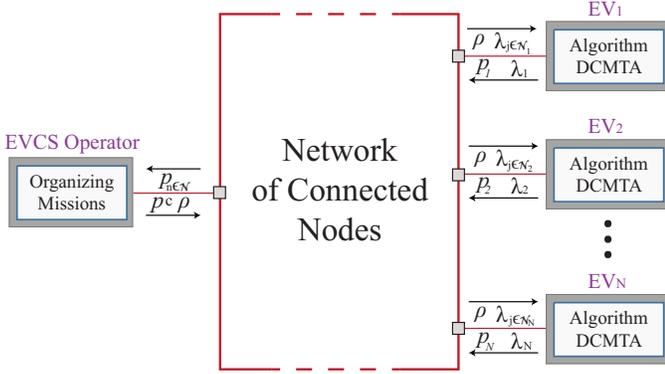


Fig. 5. The interactive communications within the network of connected nodes.

In the first task of the algorithm, initialization is performed by assigning both  $A_n^{max}$  and  $A_n^{min}$  to one for normalization and modification purposes. Afterwards, the optimization task is applied in which the  $EV_n$  finds its optimal charging pattern, i.e., schedule, individually over the the horizon time. This is achieved by solving the charging problem of  $EV_n$  respecting its own local current constraint only [as in line 3], and the findings are  $p_n$  and  $\lambda_n$ . The current constraint here refers to the upper limit of charging power  $P_n^{max}$  which may be updated [as in line 19]. Note that at this point of the first round execution of this task, the  $EV_n$  has not addressed its anxious energy nor overload cases if they occurred in EVCS, however, they will be tackled in the following two tasks.

In the modification task, the anxious energy of EV driver  $E_n^x$  is calculated on the basis of the results of the previous task, i.e.,  $p_n$ . Then,  $E_n^x$  is checked if it exceeds its threshold  $E_n^{x,th}$ , which is a predefined value and is determined by the EV driver. Note that the more the EV driver wants to be robust against an uncertain event, the lower the  $E_n^{x,th}$  is. If the current anxious energy is larger than the threshold, it means that the EV driver is not satisfied with the current  $p_n$  because this  $p_n$  is not suitable to meet his/her charging demand  $E_n^r$  given the potential occurrence of an uncertain event. Therefore, the EV driver modifies his/her time anxiety influence, as it has a direct influence on  $p_n$  and thus on  $E_n^x$ , by increasing its depth, i.e., reduces the lower limit  $A_n^{min}$  by a fixed amount  $\varepsilon_1$ . This modification is implemented in an iterative way until the EV driver succeeds in making his/her anxious energy below its threshold. In other words, the EV driver becomes satisfied with the current  $p_n$  as it is considered to be robust to meet his/her  $E_n^r$  given the potential occurrence of an uncertain event. Each iteration involves the process of re-optimization of the charging pattern, re-calculation of the current anxious energy, and re-reduction of the lower limit if the anxious energy. Once this task is completed, the resulting

charging pattern of  $EV_n$  is considered to be optimal with an acceptable remaining anxious energy.

Then, the communication task is processed in which the  $EV_n$  node communicates with others to handle the overload cases in EVCS if they occurred. To do so, the common constraint (9) is first checked over the time horizon [refer to line 10]. The algorithm terminates with the optimal solution if the constraint is not violated, i.e., no overload cases are occurred. On the other hand, if the current total power demand of EVs is bigger than the charging power capacity at any time step, the total demand will be pulled down to meet the capacity by a compromised procedure among EVs through restraining their current power demands. As explained before, this solution can be reached by requiring all  $\lambda_{n,t}$ 's of EVs to share the same global decision-making value  $\bar{\lambda}_t$ , an element of  $\bar{\lambda}$ . The procedure to do that is achieved by an interaction-based method which utilizes the consensus network concept [23], [24]. First, the surplus power demand of EVs above the power capacity, which is needed to be cut, is calculated and assigned to  $\Delta p_t$  [refer to line 15]. Then, an update on the  $\lambda_{n,t}$  of  $EV_n$  is applied by exploiting the sum of the weighted discrepancies between it and its neighbors, i.e.,  $\lambda_{j,t}$ 's, as well as the weighted surplus power  $\Delta p_t$  [as in line 17]. Note that the two weight parameters  $\beta_n$  and  $\alpha_n$  as well as  $\varepsilon_1$ ,  $\varepsilon_2$ , and  $\varepsilon_3$  are all user defined values. Once the converged value  $\bar{\lambda}_t$  is reached, the upper limit of the charging power of  $EV_n$  is updated in a similar way to (18) [refer to line 19]. After tackling the overload cases in all time steps of the time horizon,  $EV_n$  has to re-optimize its charging pattern with the updated local current constraint. The iteration process through the optimization, modification, and communication tasks remains until both the anxious energy and overload cases are completely addressed, then algorithm 1 terminates at line 11.

#### IV. SIMULATION ANALYSIS

The performance of the proposed algorithm with the time anxiety concept and the different EV driver behaviors is evaluated by two aspects. The first aims to investigate in the charging patterns of EVs, i.e., EV charging power distribution. Thus, a small scale of EVs with different case studies are introduced to clearly show the charging dynamics in an example time interval of the day. The second aspect, on the other hand, is presented to proof the influences of the proposed issues in conserving the profit of EVCS operator and the satisfactions of EVs in a large scale penetration of EVs throughout one day. The simulation configuration, which is adopted in both aspects, is set up as follows.

The capacity of the on-board battery of EVs and their charger power rates are randomly selected in the ranges 7.6–85 (kWh) and 3.3–10 (kW), respectively [19], [25]. The SoCs of these EVs at the arrival and departure times are randomly generated following a normal distribution in the ranges 0.2–0.6 (%) and 0.7–0.9 (%), respectively [26], [27]. As known, EVs can arrive to EVCS at any time and particularly during the potential peak arrival times [8]. Meanwhile, the charging time durations of EVs in EVCS are determined on the basis

**Algorithm 1** Distributed Charging Management with Time Anxiety (DCMTA)

**I. Initialization Task**

1:  $A_n^{max} = 1$

2:  $A_n^{min} = 1$

**II. Optimization Task**

3: Solve (8) subject to (10)

**III. Modification Task**

4: Calculate  $E_n^x$  by (7)

5: **if**  $E_n^x \geq E_n^{x,th}$  **then**

6:  $A_n^{min} \leftarrow A_n^{min} - \varepsilon_1$

7: Calculate  $A_n$  by (13)

8: Go back phase II

9: **end if**
**IV. Communication Task**

10: **if** ( $|\sum_{n \in \mathcal{N}} P_n - p^c| \leq \varepsilon_2$ ) **then**

11: Terminate

12: **end if**

13: **for**  $\forall t \in \mathcal{T}$  **do**

14: **while**  $\sum_{n \in \mathcal{N}} P_{n,t} > p_t^c + \varepsilon_2$  **do**

15:  $\Delta p_t = \sum_{n \in \mathcal{N}} P_{n,t} - p_t^c$

16: **while**  $\max(|\lambda_{n,t} - \lambda_{j,t}|) > \varepsilon_3$  **do**  $\forall j \in \mathcal{N}_n$ 

17:  $\lambda_{n,t} \leftarrow \lambda_{n,t} + \sum_{j \in \mathcal{N}_n} \alpha_n (\lambda_{j,t} - \lambda_{n,t}) + \beta_n \Delta p_t$

18: **end while**

19:  $P_{n,t}^{max} = \mathcal{P} \left[ \frac{\lambda_{n,t} - \rho_t \Delta t}{\rho_n^s \Delta t^2} \right]$

20: **end while**

21: **end for**

22: Go back phase II

of some issues including the predicted next travel schedules and charging demands, i.e., requirements. Hence the departure times of EVs from EVCS are randomly set with realistic consideration of these issues. The electricity price sensitivity is assumed to be 0.001 ( $\$/(\text{kWh})^2$ ) to make a suitable response to the low electricity prices, and the data profiles of temperature and solar irradiance for solar power generation, BLS load, and electricity price are adopted as in [28]–[30], respectively.

**A. Small Scale of EV Penetration**

Following the above explanation and simulation configuration, three EVs are selected here and their specifications are reported in Table I. As seen, each EV driver is assumed to have a different behavior (BEHR.) from others. The anxious time interval of each  $EV_n$  is considered to be the last hour of the charging duration, i.e.,  $t_n^d = t_n^a - 1$  (h). As shown, these EVs are scheduled to be charged during the time interval 8:00–14:00 in which the electricity price is illustrated in Fig. 6(a). In this section, three case studies are introduced that focus on different points and their results are illustrated in Fig. 6(b)–(d).

The first case study discusses the influence of the anxious energy threshold (Anx. Eng. THLD) on the EV anxiety depth and charging cost. In this regard,  $EV_3$  is selected as an example with five scenarios. Each scenario (S) has a specific demand

**TABLE I**  
SPECIFICATIONS OF THE EXAMPLE THREE EVS

SPEC	$C_n$ (kWh)	$P_n^r$ (kW)	$t_n^a$ (h)	$t_n^d$ (h)	$SoC_n^a$ (%)	$SoC_n^d$ (%)	BEHR.
$EV_1$	17	3.3	8:30	13:10	0.21	0.90	HTAD
$EV_2$	18	3.3	8:35	13:20	0.23	0.89	LTAD
$EV_3$	19	3.3	8:40	14:00	0.32	0.85	MTAD

of the anxious energy threshold as listed in Table II. Since the anxious energy threshold of  $S_1$  is large enough 3.3 (kWh), it indicates for a loose charging demand of the driver and thus he/she has no anxiety depth here, i.e., 0.00 (%). Consequently, the charging pattern of  $EV_3$  results only from the electricity price and the charging requirements. In other words,  $EV_3$  is charged with its upper limit of charging power,  $P_3^r$ , 3.3 (kW) at electricity price 0.150 ( $\$/\text{kWh}$ ) and fulfilled its charging demand at price 0.160 ( $\$/\text{kWh}$ ) with no further need to be charged at 0.180 ( $\$/\text{kWh}$ ).

For other scenarios, i.e.,  $S_2$ – $S_5$ , their charging patterns follow similar trend to that one of  $S_1$ . However, as designed in the modification task of algorithm 1, the smaller anxious energy threshold leads to a smaller value of  $A_n^{min}$ , and thus a bigger anxiety depth. In other words, the EV driver will reasonably be more anxious to reduce his/her current anxious energy to meet the demanded anxious energy threshold. Consequently,  $EV_3$  tries to shift, i.e., reschedule, more charging energy from the anxious time interval to earlier times if possible as depicted in Fig. 6(b). If the shifted energy is moved to a time interval with higher electricity price rate, an increase in the charging cost will be occurred. Thus, the charging cost of  $S_2$  is the same of  $S_1$  while the charging cost of  $S_5$  is the highest among others as the amount of its shifted energy is the highest from the electricity price 0.160 ( $\$/\text{kWh}$ ) to 0.180 ( $\$/\text{kWh}$ ). Note that if a charging cost increase is happened, it is still small and  $EV_3$  sacrifices it in order to meet its charging energy demand rather than mismatching it due to some unpredicted events when it leaves the EVCS.

**TABLE II**  
ANXIETY DEPTHS AND CHARGING COSTS OF  $EV_3$  UNDER DIFFERENT ANXIOUS ENERGY THRESHOLDS.

Scenario	$S_1$	$S_2$	$S_3$	$S_4$	$S_5$
Anx. Eng. THLD (kWh)	3.300	2.640	1.650	0.660	0.000
Anxiety Depth (%)	0.00	0.02	0.14	0.20	0.25
Charging cost (\$)	1.599	1.599	1.616	1.634	1.649

In the second case study, the effect of the EV driver behavior is discussed. The  $EV_2$  is selected here as an example and its driver behavior is changed among the NTAD, LTAD, MTAD, and HTAD for investigation purposes. The anxiety depth of  $EV_2$  driver is assumed to be 0.26 (%) and the results are shown in Table III and Fig. 6. As seen, different behaviors lead to different anxious energies and charging costs. As illustrated in the anxiety influence map of Fig. 6(c), the impact difference of HTAD is the highest, then orderly those ones of MTAD, LTAD, and NTAD, which match the discussion in section III-A. This issue results in making the anxious energy of HTAD to be the lowest, then that ones of MTAD,

LTAD, and NTAD, respectively. Note that the anxious energy of NTAD is the biggest among others because the driver is careless about this quantity. It is observed that the more anxious driver tries to shift more energy from the anxious time interval to earlier intervals to reduce his/her anxious energy. Under the example electricity profile, these earlier time intervals have electricity price 0.180 ( $\$/kWh$ ) comparing with 0.160 ( $\$/kWh$ ) of the original intervals. Thus, a small increase in the charging cost is occurred by the more anxious driver, in which it is accepted by him/her in order to secure his/her charging demand to be reached if some unpredicted circumstances are occurred near or in the anxious time interval.

TABLE III

ANXIOUS ENERGIES AND CHARGING COSTS OF  $EV_2$  UNDER DIFFERENT DRIVER BEHAVIORS.

EV Driver Behavior	NTAD	LTAD	MTAD	HTAD
Anxious Energy ( $kWh$ )	3.300	1.650	0.715	0.330
Charging cost ( $\$$ )	1.940	1.977	1.992	1.999

The third case study investigates in the charging patterns of EVs under different charging requirements, behaviors, and charging power capacities of EVCS. Here, besides of the EV specifications in Table I, their demanded anxious energy thresholds are listed in Table IV. The charging capacity of EVCS is considered here, as an example, to be 12 ( $kWh$ ) except during the time interval 9:00-9:30, in which it is set as 5.5 ( $kWh$ ). As seen from the results in Fig. 6(d), all EVs try to fulfil their charging requirements including the anxious energy thresholds at the lowest charging costs. The dynamics of the anxiety influences including the anxiety depths reflect the way of how these EVs are responding to meet their charging requirements under the charging conditions of EVCS, i.e., electricity price and charging capacity.

Since  $EV_1$  driver is HTAD and has a small, i.e., tough in demand, anxious energy threshold 0.825 ( $kWh$ ), it has a large impact difference and a wide energy depth 0.26 (%). Thus,  $EV_1$  competes more than others to make its charging power the highest during the limited charging capacity 9:00-9:30. Although  $EV_2$  has a bigger, i.e., looser to be met, anxious energy threshold than  $EV_1$ , its driver is LTAD and it has a stricter charging demand to be met, i.e., big energy demand and short charging duration. Thus, its anxiety depth is also wide 0.28 (%) and its charging power during 9:00-9:30 is between  $EV_1$  and  $EV_3$ . Finally,  $EV_3$  has loose charging requirements, i.e., small energy demand and long charging duration, as well as a moderate anxious energy threshold 1.100 ( $kWh$ ). Thus, it competes less during 9:00-9:30, and its charging power is the lowest here.

The charging cost of  $EV_3$  is the lowest due to its charging requirement and the less charging amount during the interval of high electricity price 0.180 ( $\$/kWh$ ). Although the charging cost of  $EV_1$  is similar to  $EV_2$  as they have similar charging requirements, it is a bit lower as it has more chance to be charged during the interval of low electricity price 0.150 ( $\$/kWh$ ). Note that the SoCs of EVs start from their arrival values and end up with the departure values which are listed

in Table I and their increase dynamics are proportional to their charging power amounts.

TABLE IV

CHARGING RESPONSES OF EVs UNDER A SPECIFIC CHARGING CAPACITY.

Target EV	$EV_1$	$EV_2$	$EV_3$
Anx. Eng. THLD ( $kWh$ )	0.825	1.650	1.100
Anxiety Depth (%)	0.26	0.28	0.18
Charging cost ( $\$$ )	1.968	1.975	1.635

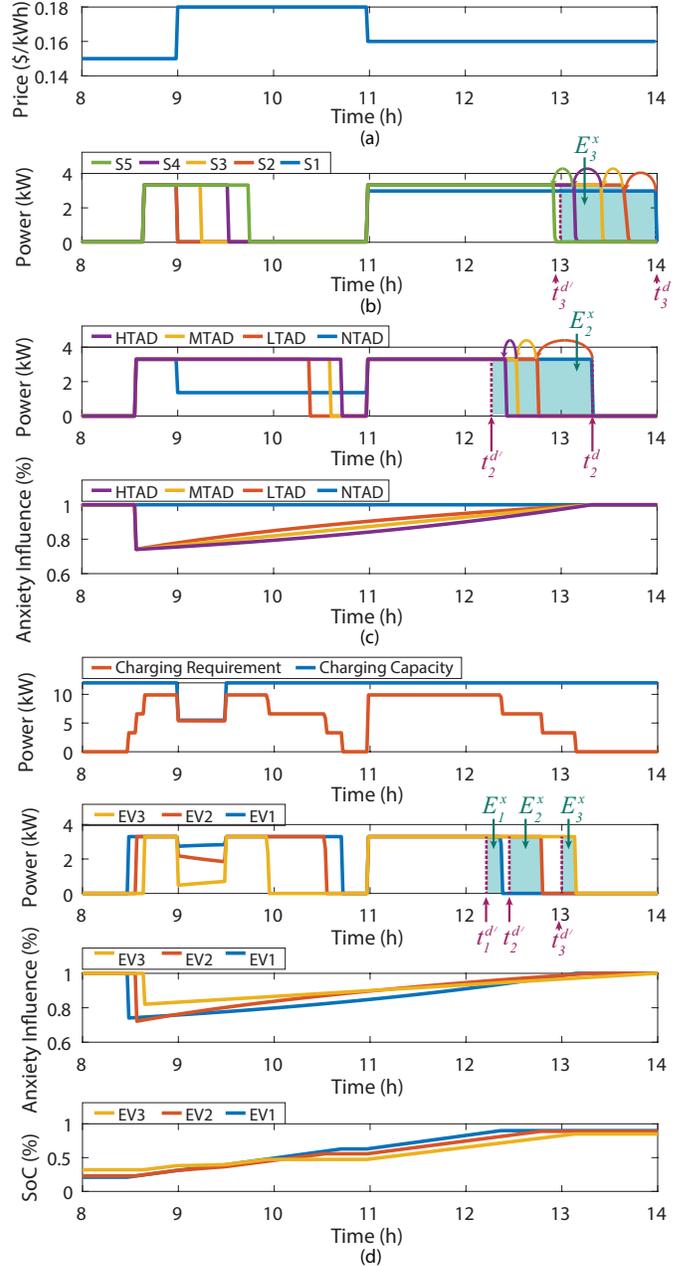


Fig. 6. (a) Electricity price profile. (b) Charging power of  $EV_2$  under different anxious energy thresholds. (c) Charging power and anxiety influence of  $EV_2$  under different driver behaviors. (d) Charging capacity, charging requirement, and EVs' responses of power, anxiety influence, and SoC.

## B. Large Scale of EV Penetration

The influences of uncertain events at different penetration numbers of EVs are discussed and evaluated. Such these events are the overloads and earlier (i.e., actual) departure times of EVs than scheduled ones which may occur near or in the anxious time intervals of EVs. The second type of events is selected here as an example in the discussion and the difference between the actual and scheduled departure times is symbolized  $\Delta t^d$  which is assumed to vary in the range  $[0, 1(h)]$ . The chosen literature method for comparison defines the EV departure time as an accurate information and does not consider a potential discrepancy that may happen on it nor its consequences [8]. In other words, this method considers the behavior of all EV drivers to be NTAD, and thus it is named as non-anxiety method (NA-M) while the proposed method is called time-anxiety method (TA-M). Moreover, two criteria are considered here for evaluation. The first is the profit of EVCS by selling charging energy to EVs. The second criterion is the satisfaction of EV driver on the charging cost and energy demand, i.e., the increase in the charging cost and the charging energy mismatch between the demanded and actual received ones [13]. A 100-run Monte Carlo simulation with different EV specifications and charging requirements at each run is adopted to give an average evaluation between the two methods.

As seen in section IV-A, EVs in TA-M are more able to fully meet their energy demands in shorter charging durations since their EV charging decisions are more robust against the departure time uncertainties. This actually has two influences. First, since the actual charging durations of EVs in TA-M are shorter than in NA-M, its service rate of EVs in one day is higher than in NA-M. The second influence is that the amount of sold energy by EVCS to EVs is higher in TA-M since its charging energy mismatches of EVs are lower than in NA-M. Thus, TA-M guarantees higher profit to EVCS than NA-M as seen in Fig. 7(a). Moreover and as seen in Fig. 7(b), TA-M conserves higher satisfactions for EVs than NA-M since EVs here are more able to meet their energy demands with no/small increase in the charging cost, as discussed in the first case study of section IV-A.

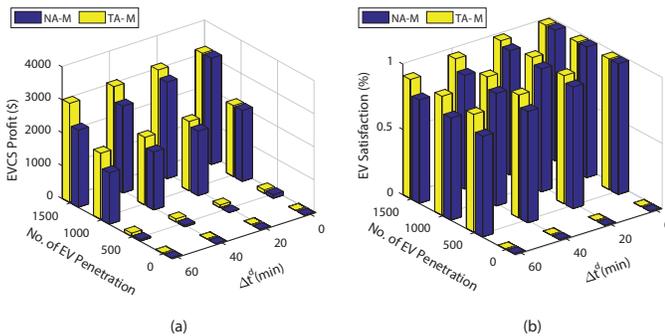


Fig. 7. Influences of departure time uncertainty and No. of EV penetration on (a) EVCS profit. (b) EV satisfaction.

## V. CONCLUSION

The behavior of EV customer plays an important role in making the charging decisions in the EV charging problem. Thus, an improved model to this behavior is significant to have more realistic and effective charging decisions. To this end, this paper proposed a time anxiety concept to mitigate the influences of some uncertain events that could happen meanwhile charging. Based on this concept, it formulated different EV customer behaviors and included them into the EV charging problem. This problem was designed as a noncooperative game and the solution was developed in a distributed way. Detailed case studies were introduced to show the influences on small and large scales. Moreover, the proposed algorithm was benchmarked against another one to further proof its performance and efficacy in securing the profit of charging facility and the satisfactions of EV customers. Consequently, the proposed charging management is worthy to be integrated in EVCS when there is a large number of EVs with different charging behaviors that usually change dynamically. Thus, the EVCS operator will be released from difficulties in collecting all the individual EV information and in applying the solution centrally in a specified interval. Furthermore, this charging management could be integrated to increase the satisfactions of the target EV customers in terms of privacy protection. This issue is important when these customers have high concerns about securing their information and behaviors.

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